



A. Box models and Residence times

Steady-state: when flow (of water, nutrients, energy) through a 'box' (a lake, the atmosphere, a population or organisms) is steady, i.e.:

> inflow (F_{in}) = outflow (F_{out}) \rightarrow box size (or stock S) doesn't change

Then residence time τ (the time it would take for the flow to fill the box if the box were empty) is the ratio of the stock in the box, to the flow:

(using consistent units)

$$\tau = \frac{S}{F} \frac{\text{grams}}{\text{grams sec}^{-1}} = sec$$







































C. Stoichiometry (proportional elemental composition, e.g. C:N:P in biomass)

Originally introduced as an ecological concept by A. Redfield in 1934 in his study of marine phytoplankton. the *Redfield ratio* , *C:N:P = 106:16:1* (relative amounts of C, N, & P in phytoplankton)

Based on what we know now about marine v terrestrial residence times (and other things we know about these systems), what might we infer/guess about terrestrial vs. marine C:N:P?

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Much more recently applied to terrestrial systems: McGroddy et al. 2004 Forest Foliage C:N:P = 1200:28:1 (Global scale) Litter = 3000:45:1 (resorption) (higher C than in marine phytoplankton: reflecting importance of carbon-rich structural components - e.g. cellulose) Next...

Thermodynamics of Biogeochemical reactions

<u>Fun problem in global biogeochemistry:</u> How likely is it that in your next breath, you will inhale at least one molecule of nitrogen (N_2) that Julius Caesar exhaled in his last breath?

(Julius Caesar, the famous Roman emperor, was assassinated on March 15, 44 BC by a group of Roman senators).

<u>This requires some basic chemistry:</u> 1 mole of air is 6.02×10^{23} molecules At STP, 1 mole occupies ~22 liters. Also helpful: whole atmosphere: 1.8×10^{20} moles of air What is atmospheric mixing ratio of N₂? What is N₂ mixing time in the atmosphere? What is N₂ residence time in the atmosphere?

From J. Harte, 2001. Consider a Cylindrical Cow

First, the concentration, in the whole atmosphere, of Caesar's last-breath $N_{\rm 2}$ molecules

 $Concentration = \frac{\#N_2 \text{ molecules in Caesar's last breath}}{\#\text{molecules in whole atmosphere}}$

$$=\frac{(1L \text{ of air in breath})\frac{3N_2}{4 \text{ air}}\left(\frac{1 \text{ mol air}}{22 \text{ Lair}}\right)(6 \times 10^{23} \text{ molecules / mol})}{(1.8 \times 10^{20} \text{ mols air / atmosphere})(6 \times 10^{23} \text{ molecules / mol})} \approx 2 \times 10^{-22}$$

Next, the average number you inhale per breath =

Concentration (molecules Caesar's N2/molecules air)×(# molecules inhaled)

$$= (2 \times 10^{-22}) \times \left[\left(1L \times \frac{1 \mod air}{22 L air} \right) (6 \times 10^{23} \mod color / mol) \right]$$
$$\approx (2 \times 10^{-22}) \times (2.7 \times 10^{22}) = 5.4 \approx 5$$

So on average you inhale 5 molecules of Caesar's-breath $N_{\rm 2}$ in every breath!

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